

Formulas:

$$(1.1) \quad q = 1.60 \cdot 10^{-19} \text{ C}; 1\text{eV} = 1.60 \cdot 10^{-19} \text{ J}$$

$$m_e = 9.1 \cdot 10^{-31} \text{ kg} = 0.511 \text{ MeV} / c^2$$

$$k_B = 1.38 \cdot 10^{-23}; R = 8.314 \text{ J} / \text{mole} \cdot \text{K} = 0.08206 \text{ Latm} / \text{mole} \cdot \text{K}; \hbar = \frac{h}{2\pi} = 1.05 \cdot 10^{-34} \text{ Js};$$

$$\sigma = 5.67 \cdot 10^{-8} \text{ (Stefan)}; \dot{Q} = eA\sigma T^4; \Delta U = nC_V \Delta T; C_P - C_V = R; \frac{1}{2} m \overline{v^2} = \frac{3}{2} k_B T; \dot{Q} = \frac{A \Delta T}{\sum \frac{L_i}{k_i}}$$

$$TV^{\gamma-1} = \text{const}; PV = Nk_B T = nRT; PV^\gamma = \text{const}; \Delta U = Q + W; \Delta S = \int_i^f \frac{dQ_r}{T}; \lambda = 1 / \sqrt{2\pi} d^2 n_V$$

$$n dE = n_0 e^{-\frac{E}{k_B T}} dE; W = - \int_{V_i}^{V_f} P dV; 1 \text{ cal} = 4.186 \text{ J}; L_{\text{water}} = 80 \text{ cal} / \text{g}$$

$$k_e = \frac{1}{4\pi\epsilon_0} = 8.89 \cdot 10^9; \epsilon_0 = 8.85 \cdot 10^{-12} \text{ S.I.}; \text{parallel plate capacitor: } E = \frac{\sigma}{\epsilon_0}; C = \kappa \frac{\epsilon_0 A}{d}$$

$$E = \frac{Q}{4\pi\epsilon_0 r^2}; \vec{E} = -\text{grad} \cdot V; \Delta V_{ab} = - \int_a^b \vec{E} \cdot d\vec{s}; C = \frac{Q}{\Delta V}; \vec{F} = q\vec{E}; U = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} C (\Delta V)^2;$$

$$dW = qdV; U_{\text{dipole}} = -\vec{p} \cdot \vec{E}; \vec{\tau} = \vec{p} \times \vec{E}; q = C\epsilon \left(1 - e^{-\frac{r}{RC}} \right); m_p = 1.67E-27 \text{ kg} = 938 \text{ MeV} / c^2$$

$$\text{coaxial: } C = L / 2k_e \ln \frac{b}{a}; I = \dot{Q} = \iint_{\text{surface}} \vec{j} d\vec{A}; \vec{j} = nq\vec{v}_d; \vec{j} = \sigma\vec{E}; \rho_\Omega = \frac{1}{\sigma}; \frac{\Delta\rho}{\rho} = \alpha\Delta T$$

$$\text{copper: } \rho_\Omega = 1.7 \cdot 10^{-8} \Omega \text{ m at } 20^\circ \text{C}; \alpha = 3.9 \cdot 10^{-5} / \text{C}^\circ; \Delta V = RI; P = I\Delta V = RI^2; \Delta V = \epsilon - rI$$

(1.2)

$$\text{div} \vec{E} = \frac{\rho}{\epsilon_0}; (1.3) \vec{F}_B = q\vec{v} \times \vec{B}$$

$$(1.4) d\vec{F}_B = I(d\vec{s} \times \vec{B}) \Rightarrow \vec{F}_B = I\vec{L} \times \vec{B}$$

$$(1.5) \vec{\mu} = I\vec{A} = \text{magnetic dipole moment}$$

$$(1.6) U_B = -\vec{\mu} \cdot \vec{B}; \vec{\tau}_B = \vec{\mu} \times \vec{B}$$

$$(1.7) \text{curl} \vec{B} = \mu_0 \vec{j}$$

$$(1.8) d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \vec{r}}{r^3} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \vec{u}_r}{r^2}; \text{Biot-Savart}; \frac{\mu_0}{4\pi} = 10^{-7}; \mu_0 = 1.2566 \cdot 10^{-6}$$

$$(1.9) \text{curl} \vec{B} = \mu_0 \left(\vec{j} + \underbrace{\epsilon_0 \frac{\partial \vec{E}}{\partial t}}_{\vec{j}_d} \right) \text{ displacement current}$$

$$(1.10) \text{ Faraday's law } \vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \quad \varepsilon = -N \frac{d\Phi_B}{dt}$$

$$(1.11) \varepsilon = -\frac{d}{dt}(\vec{B} \cdot \vec{A}) = -\frac{d}{dt}(BA \cos \theta) = -\frac{d}{dt}(BA \cos \omega t) = BA\omega \sin \omega t$$

$$(1.12) \varepsilon_L = -N \frac{d\Phi_B}{dt} = -L \frac{dI}{dt}$$

$$(1.13) L = \frac{N\Phi_B}{I}$$

$$(1.14) U_B = \frac{1}{2} LI^2 \text{ electromagnetic energy in an inductor}$$

Energy (instantaneous) density in a capacitor and coil:

$$(1.15) u_E = \frac{1}{2} \varepsilon_0 E^2; u_B = \frac{B^2}{2\mu_0}$$

ac currents

$$\hat{I}(t) = \frac{\hat{V}(t)}{\hat{Z}_{eq}}; I_{rms} = \frac{I_{max}}{\sqrt{2}}; V_{rms} = \frac{V_{max}}{\sqrt{2}}$$

$$(1.16) \hat{Z}_L = i\omega L \Rightarrow \hat{I}(t) = \frac{\hat{V}(t)}{i\omega L}; I_{max} = \frac{V_{max}}{\omega L}$$

$$\hat{Z}_C = \frac{1}{i\omega C} \Rightarrow \hat{I}(t) = i\omega C \hat{V}(t); I_{max} = \omega C V_{max}$$

$$(1.17) P = \hat{V}_{rms} \hat{I}_{rms} \cos \Phi$$

$$(1.18) \text{ In electromagnetic fields: } E = cB; u_E(t) = \frac{1}{2} \varepsilon_0 E^2; u_B(t) = \frac{1}{2\mu_0} B^2$$

Instantaneous energy density in an em wave with equal contributions from the electric field and the magnetic field:

$$(1.19) u(t)_{total} = \frac{B^2}{\mu_0} = \varepsilon_0 E^2$$

$$\bar{u}_{avg} = \frac{1}{2} \frac{B_{max}^2}{\mu_0} = \frac{\varepsilon_0}{2} E_{max}^2$$

Poynting vector, averaged over a period

$$(1.20) \bar{S}_{avg} = \frac{1}{2} \frac{E_{max}^2}{\mu_0 c} = \frac{1}{2} \frac{c B_{max}^2}{\mu_0}; \mu_0 \varepsilon_0 c^2 = 1 \quad ; \varepsilon_0 \mu_0 = \frac{1}{c^2}$$

$$(1.21) \frac{S}{c} = u = \frac{U}{V} = \frac{F dx}{A dx} = \text{pressure } P \text{ in an em-wave}$$

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$$(1.22) p = \frac{2U}{c} \text{ Perfect reflector}$$

$$(1.23) p = \frac{U}{c} \text{ Perfect absorber}$$

$$(1.24) \vec{A} \times (\vec{B} \times \vec{C}) = \vec{B} (\vec{A} \cdot \vec{C}) - \vec{C} (\vec{A} \cdot \vec{B}) \text{ for any three vectors } \vec{A}, \vec{B}, \vec{C}$$

$$(1.25) \begin{aligned} \vec{E}(x, y, z, t) &= \vec{E} = \vec{E}_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} \\ \vec{B}(x, y, z, t) &= \vec{B} = \vec{B}_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} \end{aligned}$$

$$\frac{\partial}{\partial t} (-i\omega t) = -i\omega$$

$$\vec{\nabla} \Rightarrow i\vec{k}$$

$$(1.26) \vec{\nabla} \times \vec{B} = \text{curl} \vec{B} = i\vec{k} \times \vec{B}; \vec{\nabla} \cdot \vec{B} = \text{div} \vec{B} = i\vec{k} \cdot \vec{B}$$

$$\vec{\nabla} U = \overline{\text{grad} U} = i\vec{k} U$$

$$\vec{\nabla} \cdot \vec{\nabla} = \Delta = \text{Laplace} = (i\vec{k})^2 = -k^2$$